

ΘΕΜΑ Α

- A1) α A2) γ A3) α A4) β
A5) λ, λ, λ, σ, λ

ΘΕΜΑ Β

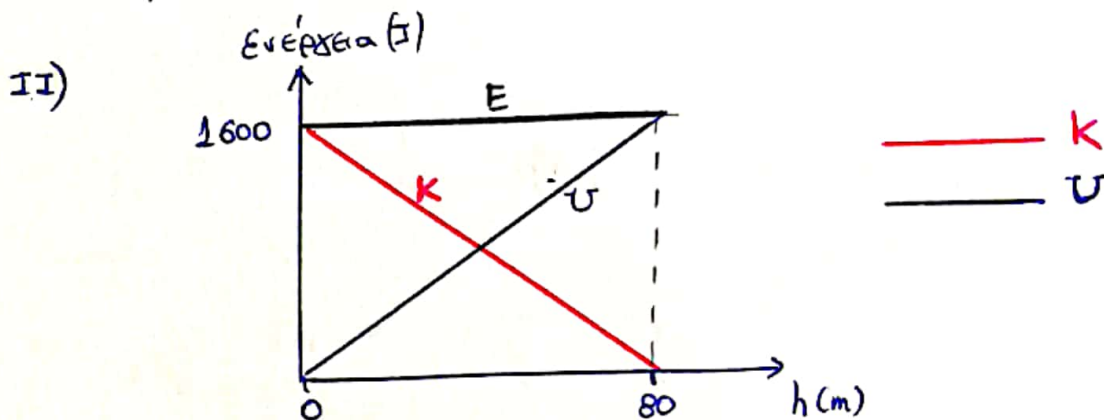
B1) $W^{A \rightarrow B} = -mgh$, $W^{B \rightarrow A} = +mgh$, $W^{A \rightarrow B \rightarrow A} = -mgh + mgh = 0$
Σωστό το (δ)

B2) I) $W_F = F \cdot \Delta x = \frac{(6+2)4}{2} J = 16 J$, Σωστό το (α)

II) $\frac{1}{2} m v^2 - 0 = W_F \Rightarrow v = \sqrt{16} \Rightarrow v = 4 \text{ m/s}$, Σωστό το (δ)

- B3) • $U_A = mgh_A = 9 \cdot 10 \cdot 80 = 1600 J$, $k_A = 0$, $E_A = k_A + U_A = 1600 J$
 • $E_B = E_A = 1600 J$, $U_B = mgh_B = 9 \cdot 10 \cdot 35 = 700 J$, $k_B = E_B - U_B = 900 J$
 $k_B = \frac{1}{2} m v_B^2 \Rightarrow v_B = 30 \text{ m/s}$, $v_B = g t_B \Rightarrow t_B = 3 \text{ s}$
 • $U_\Gamma = 0$, $E_\Gamma = E_A = 1600 J$, $E_\Gamma = k_\Gamma = 1600 J$
 $k_\Gamma = \frac{1}{2} m v_\Gamma^2 \Rightarrow v_\Gamma = 40 \text{ m/s}$, $v_\Gamma = g t_\Gamma \Rightarrow t_\Gamma = 4 \text{ s}$

ΘΕΣΗ	h (m)	k (J)	U (J)	v (m/s)	t (s)
A	80	0	1600	0	0
B	35	900	700	30	3
Γ	0	1600	0	40	4



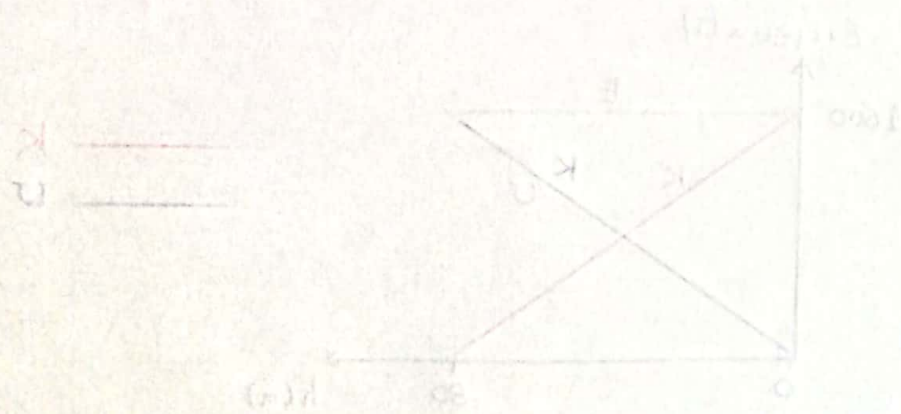
B4) • $\frac{1}{2} m u_1^2 - 0 = W_1$ (1)

• $\frac{1}{2} m u_2^2 - 0 = W_2 \Rightarrow \frac{1}{2} m (2u_1)^2 - 0 = W_2 \Rightarrow 4 \frac{1}{2} m u_1^2 = W_2 \stackrel{(1)}{\Rightarrow}$

$\Rightarrow 4W_1 = W_2 \Rightarrow W_2 = 4W_1$

Σ WGR to (a)

Year	Revenue (₹)	Cost (₹)	Profit (₹)	Loss (₹)
0	0	0	0	0
1	100	50	50	0
2	400	100	300	0
3	900	150	750	0



ΘΕΜΑ Γ

Γ1) 0-2s

ε-ο. ΕΠΙΤΑΧΥΝΩΜΕΝΗ.Κ

$$\Delta x_1 = s_1 = E_1 = \frac{(8+4)2}{2} \text{ m} = 12 \text{ m}$$

$$a_1 = \frac{\Delta v_1}{\Delta t_1} = 2 \text{ m/s}^2$$

2s-6s

ε-ο.κ.

$$\Delta x_2 = s_2 = E_2 = 4 \cdot 8 \text{ m} = 32 \text{ m}$$

$$a_2 = 0$$

6s-8s

ε-ο. ΕΠΙΒΡΑΔΥΝΩΜΕΝΗ.Κ

$$\Delta x_3 = s_3 = E_3 = \frac{2 \cdot 8}{2} \text{ m} = 8 \text{ m}$$

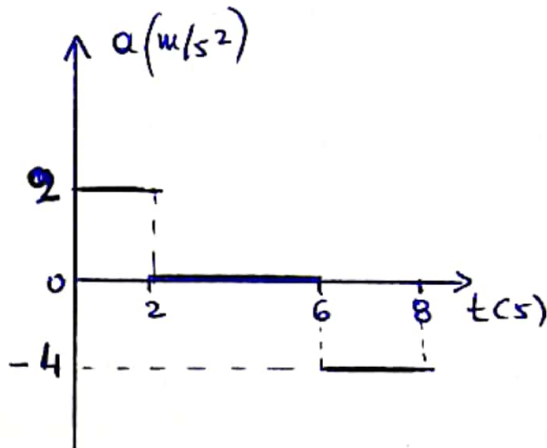
$$a_3 = \frac{\Delta v_3}{\Delta t_3} = -4 \text{ m/s}^2$$

β) $S_{\text{ολ}} = s_1 + s_2 + s_3 = 52 \text{ m},$

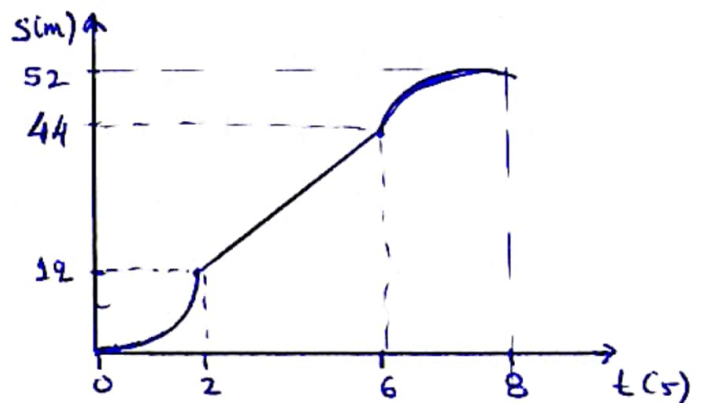
$$v_{\mu} = \frac{S_{\text{ολ}}}{t_{\text{ολ}}} = \frac{52}{8} \Rightarrow \boxed{v_{\mu} = 6,5 \text{ m/s}}$$

Γ2)

α)



β)



Γ3) $W_{T_{\text{ολ}}} = -T \cdot S_{\text{ολ}} = -10 \cdot 52 \text{ J} = -520 \text{ J}$

$$Q_{\text{ολ}} = |W_{T_{\text{ολ}}}| = 520 \text{ J}$$

Γ4) Για $t_1 = 3 \text{ s}$: $v_1 = v_0 + a_1 \Delta t_1 = 4 + 2 \cdot 1 \Rightarrow v_1 = 6 \text{ m/s}$

Για $t_2 = 7 \text{ s}$: $v_2 = v_0 - |a_3| \cdot \Delta t_2 = 8 - 4 \cdot (7-6) \Rightarrow v_2 = 4 \text{ m/s}$

$$\frac{k_1}{k_2} = \frac{\frac{1}{2} m v_1^2}{\frac{1}{2} m v_2^2} = \frac{6^2}{4^2} = \frac{36}{16} = \frac{9}{4}$$

ΘΕΜΑ Δ

Για το κεκλιμένο επίπεδο:

$$W_1 = m_1 g = 100 \text{ N}, \quad W_{1x} = W_1 \cdot \eta \cdot \phi = 100 \cdot 0,6 = 60 \text{ N}, \quad W_{1y} = W_1 \cdot \sigma \cdot \phi = 80 \text{ N}$$

$$\Sigma F_y = 0 \Rightarrow N = W_{1y} \Rightarrow N = 80 \text{ N}, \quad T_1 = \mu \cdot N_1 = 0,5 \cdot 80 \Rightarrow T_1 = 40 \text{ N}$$

$$\Delta 1) \cdot W_W = W_{W_{1x}} = W_{1x} \cdot s \Rightarrow W_W = 60 \cdot 4 \text{ J} \Rightarrow \boxed{W_W = +240 \text{ J}}$$

$$\eta \cdot \phi = \frac{h}{s} \Rightarrow s = \frac{h}{\eta \cdot \phi} = \frac{2,4}{0,6} \text{ m} \Rightarrow s = 4 \text{ m}$$

$$\cdot W_{T_1} = -T_1 \cdot s = -40 \cdot 4 \text{ J} \Rightarrow \boxed{W_{T_1} = -160 \text{ J}}$$

$$\Delta 2) \text{ ΘΜΚΕ } \frac{1}{2} m v_1^2 - 0 = W_{W_{1x}} + W_{T_1} \Rightarrow \frac{1}{2} \cdot 10 v_1^2 = 240 - 160 \Rightarrow$$

$$5 v_1^2 = 80 \Rightarrow v_1^2 = 16 \Rightarrow v_1 = \sqrt{16} \Rightarrow \boxed{v_1 = 4 \text{ m/s}}$$

$$\text{η ΘΜΚΕ } K_1 - 0 = W_{W_{1x}} + W_{T_1} \Rightarrow \boxed{K_1 = 80 \text{ J}}$$

Για το οριζόντιο επίπεδο

$$\Sigma \text{ΘΜΑ } m_1 \quad \Sigma F_y = 0 \Rightarrow N_1' = W_1 = 100 \text{ N}, \quad T_1' = \mu \cdot N_1' = 50 \text{ N}$$

$$\Sigma F_x = m a_1 \Rightarrow T_1' = m a_1 \Rightarrow a_1 = 5 \text{ m/s}^2 \text{ (Μέτρο επιβράδυνσης)}$$

$$\text{Για } t_1 = 0,8 \text{ s} : s_1 = v_0 t_1 - \frac{1}{2} a_1 t_1^2 \Rightarrow s_1 = 4 \cdot 0,8 - \frac{1}{2} \cdot 5 \cdot 0,8^2 \Rightarrow \boxed{s_1 = 1,6 \text{ m}}$$

$$\text{Όπως } t_1 = t_{\text{stop}} = \frac{v_0}{a_1} = 0,8 \text{ s} \text{ ορα να } s_1 = s_{\text{stop}} = 1,6 \text{ m.}$$

ΣΘΜΑ m₂

$$F_x = F \sigma \cdot \phi = 50 \cdot 0,8 \Rightarrow F_x = 40 \text{ N}, \quad F_y = F \eta \cdot \phi = 50 \cdot 0,6 \Rightarrow F_y = 30 \text{ N}$$

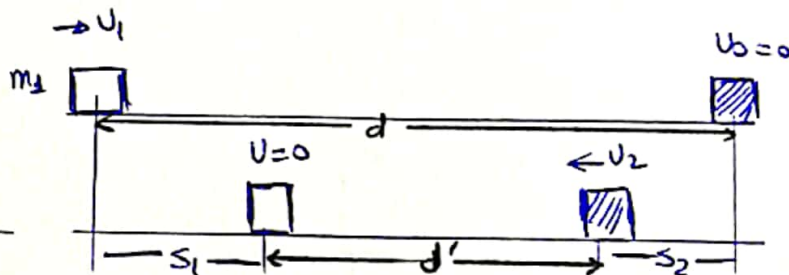
$$\cdot \Sigma F_y = 0 \Rightarrow N_2 + F_y = W_2 \Rightarrow N_2 = W_2 - F_y \Rightarrow N_2 = 50 \text{ N} - 30 \text{ N} \Rightarrow N_2 = 20 \text{ N}$$

$$T_2 = \mu \cdot N_2 = 0,5 \cdot 20 \text{ N} \Rightarrow T_2 = 10 \text{ N}$$

$$\cdot \Sigma F_x = m_2 a_2 \Rightarrow F_x - T_2 = m_2 a_2 \Rightarrow 40 - 10 = 5 \cdot a_2 \Rightarrow a_2 = 6 \text{ m/s}^2$$

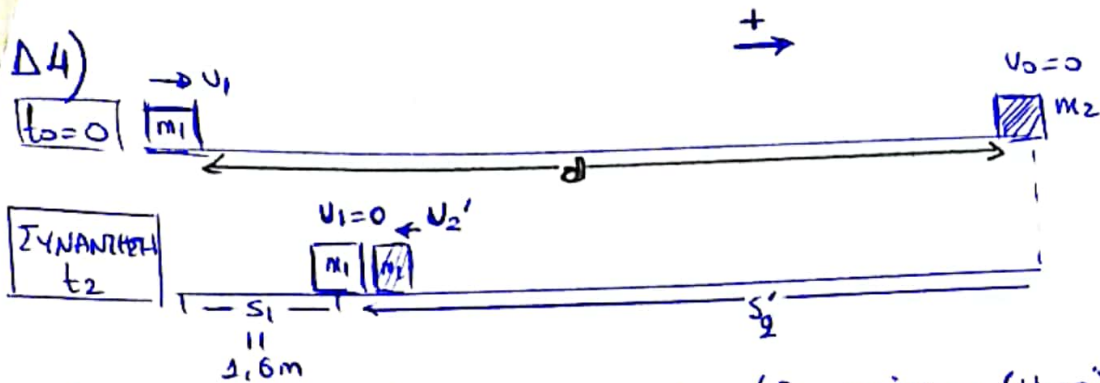
$$\cdot \text{Για } t_1 = 0,8 \text{ s} : s_2 = \frac{1}{2} a_2 t_1^2 = \frac{1}{2} \cdot 6 \cdot 0,8^2 \Rightarrow \boxed{s_2 = 1,92 \text{ m}}$$

$$\boxed{t_0 = 0}$$



Δ3)

$$d' = d - s_1 - s_2 \Rightarrow d' = 49,6 \text{ m} - 1,6 \text{ m} - 1,92 \text{ m} \Rightarrow \boxed{d' = 46,08 \text{ m}}$$



- Όταν γίνει η σύγκρουση το m_1 είναι ήδη ακίνητο. ($v_1=0$)
- Το m_2 από τη $t_0=0$ έως τη στιγμή t_2 ως σώμα ελεύθερο έχει διατρέξει διάστημα $s_2' = d - s_1 = 49,6\text{m} - 1,6\text{m} \Rightarrow s_2' = 48\text{m}$
- $s_2' = \frac{1}{2} a_2 t_2^2 \Rightarrow 48 = \frac{1}{2} \cdot 6 \cdot t_2^2 \Rightarrow t_2^2 = 16 \Rightarrow t_2 = \sqrt{16} \Rightarrow \boxed{t_2 = 4\text{s}}$
- και $|v_2'| = a_2 t_2 = 6 \cdot 4 \text{ m/s} \Rightarrow |v_2'| = 24 \text{ m/s}$ ή $v_2' = -24 \text{ m/s}$ (αλγεβρική τιμή)

